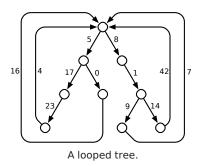
- 1. Describe and analyze an algorithm to compute the shortest path from vertex s to vertex t in a directed graph with weighted edges, where exactly *one* edge $u \rightarrow v$ has negative weight. Assume the graph has no negative cycles. [Hint: Modify the input graph and run Dijkstra's algorithm. Alternatively, **don't** modify the input graph, but run Dijkstra's algorithm anyway.]
- 2. You just discovered your best friend from elementary school on Twitbook. You both want to meet as soon as possible, but you live in two different cites that are far apart. To minimize travel time, you agree to meet at an intermediate city, and then you simultaneously hop in your cars and start driving toward each other. But where *exactly* should you meet?

You are given a weighted graph G = (V, E), where the vertices V represent cities and the edges E represent roads that directly connect cities. Each edge e has a weight w(e) equal to the time required to travel between the two cities. You are also given a vertex p, representing your starting location, and a vertex q, representing your friend's starting location.

Describe and analyze an algorithm to find the target vertex *t* that allows you and your friend to meet as soon as possible, assuming both of you leave home *right now*.

To think about later:

3. A *looped tree* is a weighted, directed graph built from a binary tree by adding an edge from every leaf back to the root. Every edge has a non-negative weight.



- (a) How much time would Dijkstra's algorithm require to compute the shortest path between two vertices *u* and *v* in a looped tree with *n* nodes?
- (b) Describe and analyze a faster algorithm.