A subsequence is anything obtained from a sequence by deleting a subset of elements; the elements of the subsequence need not be contiguous in the original sequence. For example, the strings I, PRO, DAMMM, NROAIG, and DYNAMICPROGRAMMING are all subsequences of the string DYNAMICPROGRAMMING.

- 1. Suppose we are given two arrays A[1..m] and B[1..m]. A common subsequence of A and B is any subsequence of A that is also a subsequence of B. For example, AMI is a common subsequence of DYNAMIC and PROGRAMMING. Describe and analyze an efficient algorithm to compute the length of the *longest* common subsequence of A and B.
- 2. Describe and analyze an efficient algorithm to compute the length of the longest common subsequence of *three* given arrays A[1..l], B[1..m], and C[1..n].
- 3. A *shuffle* of two strings *X* and *Y* is formed by interspersing the characters into a new string, such that the characters of *X* and *Y* remain in the same order. For example, given the strings 'dynamic' and 'programming', the string 'prodgyrnamammiincg' is indeed a shuffle of the two:

Given three strings A[1..m], B[1..n] and C[1..m+n], describe an algorithm to determine whether C is a shuffle of A and B.

In all cases, first describe a recursive algorithm and only then transform it into an iterative algorithm.